

Design and Optimization of a 10 nH Square-Spiral Inductor for Si RF Ics.

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Abstract

Nowadays, as the demand for wireless communication continues to expand, the need for high quality (Q) inductors for high-level integration of RF circuit, in order to reduce cost, has become more important. Recently, many research activities have been focused on the design, model and optimization of spiral inductors on silicon substrate. However, most of the reported Q of spiral inductors is limited to below 10 at giga hertz range. In this project, the Si IC spiral inductor is analyzed using electromagnetic analysis. With appropriate approximations, the calculations are reduced to electrostatic and magnetostatic calculations. The important effects of substrate loss are included in the design. Classical circuit analysis and network analysis techniques are used to derive twoport parameters from the circuits. This analysis is applied to traditional square inductor structure.

Introduction

Modern silicon integrated circuits are finding wide application in the GHz frequency range. The CMOS and BiCMOS processes provide high f_T transistors allowing Si RF-ICs to compete with GaAs ICs in the important low GHz frequency ranges. However, the lossy Si substrate makes the design of high Q reactive components difficult. Despite this difficulty, the low cost of Si IC fabrication over GaAs IC fabrication and the potential for integration with baseband circuits makes Si the process of choice in many RF IC applications.

The demands placed on wireless communication circuits include low supply voltage, low cost, low power dissipation, low noise, high frequency of operation and low distortion. These design requirements cannot be met satisfactorily in many cases without the use of RF inductors. Hence, there is a greatly incentive design, optimize, and model spiral inductors fabricated on Si substrates. Typical applications of on-chip inductors include low loss inductors for input matching of low noise amplifiers, inductively loaded pre-amplifiers, output matching networks for high efficiency switch-mode power amplifiers, and high Q tank circuits for low phase noise voltage control oscillators. The design has included higher conductivity metal layers to reduce the loss resistance of inductor. The use of multi-metal layers to increase the effective thickness of the spiral inductor and thereby reduce loss. The connection of multi-metal layer spirals in series to reduce the area of the inductors, the low-loss substrates to reduce losses in the substrate at high frequency, and thick oxide or floating inductors to isolate the inductor from the lossy substrate.

In an analysis approach is presented where an equivalent circuit for each segment of the spiral is calculated and the inductor is considered as an interconnection of such segments. The approach is limited, though, as many important effects are not included. For instance, non-uniform current distribution due to skin and proximity effects within each segment is not considered. In addition, the impedance to substrate is calculated using a 2-dimensional approach, making it difficult to apply to arbitrary structures or to coupled inductors.

Most past researchers have used measurement results on previously built inductors to construct models. While this technique is most practical, it does not allow the possibility of optimization nor does it allow the circuit designer freedom to choose parameters such as inductance, capacitance and Q. Otherwise researchers have used commercial 3D electromagnetic simulators to design and analyze inductors. While this approach is accurate, it can be computationally very expensive and time-consuming. This design presents an accurate and computationally efficient approach to overcome the requirement.

Project Overview

Since square spiral inductors are the most common in Si RF IC's. So, the target of this project is to design a 10nH square spiral inductor with high quality factor (Q). The solution is to find the number of turns and all dimensions of the square spiral inductor. Another importance part of the spiral inductor is the substrate. The quality factor of spiral inductor depends on the materials that constructed from substrate. So, another problem is to find the materials to design that substrate that produces a high quality factor and low cost.

1. Background

The inductance of a planar spiral square inductor can be calculated according to the Greenhouse theory. Basically, the spiral square inductor is split up into sections consisting of straight conductors, and the self-inductance of the sections is calculated and summed up. Beside the consideration of the self-inductance of each straight conductor, the mutual inductance (positive or negative) between parallel segments needs to be included for the calculation of the overall inductance.

1.1 Self-Inductance

The self-inductance for a straight conductor is,

$$L = 0.002l \left[ln \left(\frac{2l}{GMD} \right) - 1.25 + \frac{AMD}{l} + \left(\frac{\mu}{4} \right) \Gamma \right]$$
(1)

Where L is the self-inductance in microhenries, l is the conductor length in cm, GMD and AMD represent the geometric and arithmetic mean distance, respectively, of the conductor cross section, μ is the conductor permeability, and T is the frequency-correction parameter.

The geometric mean distance (GMD) between two conductors is the distance between two infinitely thin imaginary filaments whose mutual inductance is equal to the mutual inductance between the two original conductors (fig. 1b). The GMD is equal to 0.44705 times a side in the case of a square cross section.

The arithmetic mean distance (AMD) is the average of all the distances between the points of one conductor and the points of another. For a single conductor, the arithmetic mean distance is the average of all possible distances within the cross section.



Fig. 1a. Layout of current filaments.

Fig. 1b. Two parallel-filament geometry.

If we usr the top layer of metal for the layout of the spiral inductor, we can consider it as a thin-film inductor with rectangular cross section and equation (1) takes the form

$$L = 0.002l \left[ln \left(\frac{2l}{a+b} \right) + 0.50049 + \frac{a+b}{3l} \right]$$
(2)

Where a, b are the rectangular dimension of the cross section. The magnetic permeability μ is 1, and the skin-depth phenomenon has little effect on thin film, T should be considered to have a value of 1 for microwave frequencies.



Fig. 2. Layout of a typical rectangular spiral inductor.

Table.1 Variation in Frequency-Correction Parameter T for Thin Films and Microwave Frequencies.

Value of T	Film Thickness	Frequency
0.9974	10,000 angstroms	10 gigahertz
0.9986	0.0025 millimeter (0.1 mil)	1 gigahertz
0.9095	0.0075 millimeter (0.7 mil)	1 gigahertz

1.2 Mutual inductance

In the case of an L-shaped thin-film inductor, total inductance is equal to the sum of the self-inductance of the two straight segments, and less than the inductance of a single straight track of equal length. In the case of a rectangular of square planar coil, straight conductor segments are parallel to other straight conductor segments, and the mutual inductance between these parallel tracks contributes to the total inductance of the coil. Figure.2 shows the top view of a 3-turn spiral inductor. For a typical process with two layers of metal, the top layer is used for forming the spiral inductor and the bottom layer for routing the inner turn outward. As the metal layer is separated from the substrate with an oxide layer, so the top layer is used for the inductor layout so as to increase the oxide thickness from the ground so that the substrate effect will be reduced and the selfresonant frequency improved. Secondly, the top layer has a thicker layer of metal of metal which help to reduce both the dc and high frequency resistance so that factor of the inductor can be improved.

The inductance of the spiral in Fig.1 is equal to the sum of the self-inductance for each segment in the coil plus the mutual inductance, which are determined by the geometry and the phase relationship between the current carried by those lines. Figure 3 shows the model of two straight conductors carrying in-phase or out-of-phase current. There is a mutual inductance of M between the two conductors. For in-phase current such



Fig.3 Modeling of two conductors carrying in-phase and out-of-phase current

as the current in segment 1 and 5 of the inductor in figure 2, two equations (shown below) govern the voltages and currents in the two conductors,

$$V_0 = I_1(jw\omega L) + I_2(jw\omega LM)$$
(3)

$$V_1 = I_2(jw\omega L) + I_1(jw\omega LM)$$
(4)

and for in phase current ($V_1 = V_2$). After manipulation of the equation (3) and (4), one can calculate that the impedance Z_{in} of segment 1 is,

$$Z_{in} = jw\omega(L+M) \tag{5}$$

which means the inductance of the conductor increases by M, and M is the mutual inductance between the two conductors. So, parallel currents travelling in phase can contribute positive mutual components of inductance. For the case of out-of-phase current, such as current in segment 5 and 7, the calculation of the impedance Z_{in} is almost the same but now $V_1 = -V_0$ and will contribute negative mutual components of inductance. Thus the inductance of a conductor can be expressed as,

$$\mathbf{L} = \mathbf{L}_{\text{self}} \pm \mathbf{M} \tag{6}$$

The mutual inductance between two parallel conductors is a function of the length of the conductors and of the geometric distance between them. In general,

$$\mathbf{M} = 2\mathbf{I}\mathbf{Q} \tag{7}$$

where M is the mutual inductance in nH, 1 is the conductor length in cm, and Q is the mutual inductance parameter calculated from the equation

$$Q = \ln\left[\frac{1}{GMD} + \sqrt{1 + \frac{l^2}{(GMD)^2}}\right] - \sqrt{1 + \frac{(GMD)^2}{l^2}} + \frac{GMD}{l}$$
(8)

where GMD, the geometric mean distance between the two conductors, is approximately equal to the distance between the track center. The exact value of the GMD is,

$$\ln GMD = \ln d - \left[\frac{1}{12\left(\frac{d}{w}\right)^2} + \frac{1}{60\left(\frac{d}{w}\right)^4} + \frac{1}{168\left(\frac{d}{w}\right)^6} + \frac{1}{360\left(\frac{d}{w}\right)^8} + \frac{1}{660\left(\frac{d}{w}\right)10} + \dots\right]$$
(9)

where d is the center to the center separation between the conductors, and w is the width of the conductors.

For two parallel conductors with lengths of j and m (Fig.1b), the total mutual inductance can be represented by

$$2M_{j,m} = (M_{m+p} + M_{m+q}) - (M_p + M_q)$$
(10)

and the individual M terms are calculated using equation (7) and the lengths corresponding to the subscript, which is

$$M_{m+p} = 2l_{m+p} Q_{m+p} = 2(m+p)Q_{m+p}$$
(11)

where $Q_{m + p}$ is the mutual-inductance parameter Q for GMD/(m + p). The total inductance of the spiral in figure.2, which neglects the extra routing segments, is the sum of the self-inductances of each of the straight segments (L₁..L_n) plus all the mutual inductances between the segments, which is

$$L_{\rm T} = L_0 + M_+ + M_- \tag{12}$$

where L_T is the total inductance, L_0 is the sum of the self-inductances of all straight segments, M ₊ is the sum of the positive mutual inductances and M ₋ is the sum of the negative mutual inductances.

1.3 Skin depth effect

The resistance of a metal segment will increase as frequency rises due to the skin depth effect. The skin depth of metal is shown below,

$$\delta = \sqrt{\frac{\rho}{\pi\mu f}}$$
(13)

where δ is the skin depth, ρ is the frequency and μ is the permeability of free space, $4\pi \times 10^7$. The skin resistance R_s is,

$$R_{s} = \frac{\rho}{\delta}$$
(14)

For aluminum, the skin depth is approximately $1.2\mu m$ at 5GHz, roughly the thickness of metal lines in IC fabrication process. This implies that the series resistance of the spiral would not deviated much from its DC value up to 5GHz. For this reason, the skin depth effect will be ignored in the design.

1.4 Inductor Quality Factor

The quality of an inductor is measured by its Q, which is defined as

$$Q = 2\pi \frac{\text{energy stored}}{\text{energy loss in one oscillation cycle}}$$
(15)

For an inductor, only the energy stored in the magnetic field is of interest. Any energy stored in the inductor's electric field, because of some inevitable parasitic capacitances in a real inductor, is a loss. Hence, Q is proportional to the net magnetic energy stored, which is equal to the difference between the peak magnetic and electric energies. An inductor is at self-resonance when the peak magnetic and electric energies are equal. Therefore, Q vanishes to zero at the self-resonance frequency. Above the self-resonance frequency, no net magnetic energy is available from an inductor to any external circuit. To be more detail, the inductor Q can be defined as,

$$Q = 2\pi \frac{\text{peak magnetic energy - peak electric energy}}{\text{energy loss in one oscillation cycle}} = \frac{R}{\omega L} \left| 1 - \left(\frac{\omega}{\omega_0} \right)^2 \right|$$
(16)

which equals zero at $\omega = \omega_0$, and is less than zero beyond ω_0 . In terms of impedance, Q is equal to the ratio of the imaginary to the real part of the circuit impedance. The circuit impedance is inductive below ω_0 and capacitive above ω_0 .

In some simple RF circuits, Q can be found by equations



For parallel circuit

$$Q = \frac{Rp}{|Xp|}$$
(17)

and for serial circuit

$$Q = \frac{|Xs|}{Rs}$$
(18)

2. Physical Inductor Model



Fig. 5 Equivalent circuit of a spiral inductor

Each segment of the inductor is modeled with a two-port network consisting of elements, as shown in figure 5. Two coupled micro-strips in a typical silicon process are drawn in figure 6. The geometry characteristics of interest are the track width w of the spiral; the distance between two adjacent parallel tracks s and the height of the metal track t. the height of the Si substrate and the SiO₂ insulator are h_{Si} and h_{SiO_2} respectively. The main elements of the two-port are the series inductance L_S , the resistance R_S of the segment and the capacitors C_p formed by the insulating SiO₂ between the inductor and the Si substrate. All equations are shown below

$$\mathbf{R}_{\mathrm{S}} = \mathbf{R}_{\mathrm{sh}} \frac{1}{\mathrm{w}} \tag{19}$$

$$C_{p} = \varepsilon_{o}\varepsilon_{r} \frac{W}{h_{si}}$$
(20)

$$R_{sub} = \rho_{Si} \frac{1}{wh_{Si}}$$
(21)

where R_{sh} is the sheet resistance of the metal track. All lengths are in cm, while inductance is in nH and capacitance in pF. In this circuit, L_S models the self and mutual inductances in the second-metal segments, R_S is the accumulated sheet resistance, C_P models the parasitic capacitance from the second-metal layer to the substrate, and R_P represents the resistance of the conductive Si substrate. If one side of the inductor is grounded, the self-resonant frequency of the spiral inductor can be derived from the equivalent circuit. It is approximately equal to

$$\omega_{\rm R} = \frac{1}{\sqrt{L_{\rm S}C_{\rm P}}} \left[\frac{1 - {R_{\rm S}}^2 \left(\frac{C_{\rm P}}{L_{\rm S}}\right)}{1 - {R_{\rm P}}^2 \left(\frac{C_{\rm P}}{L_{\rm S}}\right)} \right]^{\frac{1}{2}}$$
(22)

Beyond the resonant frequency, the inductor becomes capacitive. Frequency ω_R is limited by C_P , which is inversely proportional to the oxide thickness between the second-metal layer and the substrate.

3. The Design of 10nH Square Spiral Inductor

This design is based on the background and equations that are introduced from previous sections. In this design, the 2μ m-process will be used to fabricate the chip. So, all the design specifications have met for the process. There are a lot of math equations involved the project. To simplify the problem, MathCad program was used to approach the result. That program is shown below.

$$t := 0.0001 \text{ cm} \qquad s := 0.0004 \text{ cm} \qquad w := 0.0006 \text{ cm} \qquad l_1 := 0.0213 \text{ cm} \qquad N := 7 \quad (\text{inputs})$$

$$k := 4 \cdot N$$

$$r := 2.. (2 \cdot N)$$

$$l_2 := l_1 \qquad l_3 := l_1$$

$$l_{2\tau-1} := l_2 - (r-1) \cdot (w+s)$$

$$l_{2\tau-1} := l_1 - (r-2) \cdot (w+s)$$

$$length := \sum_{y=1}^{k} l_y$$

$$l_1 = 0.0213$$

$$l_2 = 0.0213$$

$$l_3 = 0.0213$$

$$l_4 = 0.0203 \quad \text{cm}$$

$$length = 0.4274 \quad \text{cm}$$

$$y := 1.. k$$

$$L_y := 0.002 l_y \cdot \left[ln \left[2 \cdot \frac{l_y}{(w+t)} \right] + 0.50049 + \left(\frac{w+t}{3 \cdot l_y} \right) \right]$$

$$L_0 := \sum_{y=1}^{k} 10^3 \cdot L_y$$

 $L_0 = 3.6982$ nH





M1m:= sum1m 0

for
$$j \in 1..k$$

for $n \in 1..N$
$$\left| sum1m - sum1m + 2 \cdot l_{j+4n} \cdot \left[ln \left[\frac{l_{j+4n}}{GMDl_{j,(j+4n)}} + \left[1 + \left[\frac{l_{j+4n}}{GMDl_{j,(j+4n)}} \right]^2 \right]^{0.5} \right] - \left[1 + \left[\frac{GMDl_{j,(j+4n)}}{l_{j+4n}} \right]^2 \right]^{0.5} + \frac{GMDl_{j,(j+4n)}}{l_{j+4n}} \right] \right]$$

0 otherwise
sum1m

if $(j+4\cdot n) \leq k$

if $(j+4\cdot n) \leq k$

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 $l_{j+4\cdot n-2}$

$$2p := \sup 2p \leftarrow 0$$

for $j \in 1...k$
for $n \in 1...N$
$$\left\| \sup 2p \leftarrow \sup 2p + 2 \cdot (l_j - l_{j+4:n-2}) \cdot \left[\ln \left[\frac{l_j - l_{j+4:n-2}}{2 \cdot GMD2_{j,(j+4:n-2)}} + \left[1 + \left[\frac{l_j - l_{j+4:n-2}}{2 \cdot GMD2_{j,(j+4:n-2)}} \right]^2 \right]^{0.5} \right] - \left[1 + \left[\frac{2 \cdot GMD2_{j,(j+4:n-2)}}{l_j - l_{j+4:n-2}} \right]^2 \right]^{0.5} \right]$$

0 otherwise
sum2p

$$\mathbf{I} + \frac{2 \cdot GMD_{j}^{2} (j+4 \cdot n-2)}{l_{j} + 4 \cdot n - 2} \text{if } (j+4 \cdot n-2) \leq k$$



if $(j+4\cdot n-2) \leq k$

$$Ltt := L_0 + M1 - M2$$

Ltt = 10.0232 nH

Rsh := 0.03 $\frac{\text{ohm}}{\text{sq}}$ er := 3.9 eo := $\frac{10^{-9}}{36\cdot\pi}$ psi := 0.1 ohm · cm hsi := 0.03 cm hsio := 0.0003 cm

$$Rsub_{y} := \frac{\rho si \cdot l_{y}}{w \cdot hsi}$$
$$Rp := \sum_{y=1}^{k} Rsub_{y}$$

$$Rs := \frac{\text{length}}{w} \cdot Rsh$$

$$Rs = 21.37 \quad \text{ohms}$$

$$Rp = 2.3744 \cdot 10^3 \quad \text{ohms}$$

$$Cp := \varepsilono \cdot \varepsilon r \cdot \frac{w}{hsi}$$

$$Cp = 6.8967 \cdot 10^{-13} \quad F$$

The results from MathCad are shown in the table.2 and table.3 below

Table.2

The geometric values of square-spiral inductor from Mathcad.

Thickness t (µm)	Space between segments s (µm)	Width W (µm)	Outer length $l_1 (\mu m)$	Number of turns	Total Inductance L (nH)
1	4	6	213	7	10.02

The $5\frac{1}{4}$ turns that means square spiral inductor has 21 segments, which shown in figure

Tabl	le.3
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R _S (ohms)	R _P (ohms)	C _P (pF)	$\omega_{\rm R}$ (rad/s)
21.37	2.1K	0.7	3.8×10 ⁵

The two-port circuit of the 10nH square-spiral inductor can be represented as figure 6.



Fig.6: Equivalent circuit of the 10nH Square-Spiral Inductor.

The S_{11} -parameter of the two-port network above is plotted on Smith chart, which is shown in attachment. Finally, The physical of the spiral inductor will be fabricated as the figure.7a and figure.7b in attachment.



Fig.7a: Parallel coupled spiral segments over Si substrate.



Fig.7b: Layout of Spiral inductor and probe pads for measurement.

The quality Q of this Spiral Inductor is changing as a function of frequency, which is shown in figure.8.



Fig. 8: The quality Q factor of Spiral Inductor Vs frequency.

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Figure 8 shows that the quality factor Q has the maximum value of 5 at frequency 3.2 GHz. At high frequencies, when the substrate impedance is smaller than the inductive impedance of the spiral, the substrate loss dominates and the Q is a decreasing function of frequency. That is why the plot of factor Q has a peak value. This is importance because the Spiral Inductor can be designed to have a peak Q at the frequency of interest.



The Lump Circuit Simulation on HPADS

Fig. 8: Lump-circuit for simulation.



Fig.9: S₁₁ parameter on Smith Chart

The Spiral Inductor Layout From HPADS



Fig.10. Spiral-inductor layout from HPADS program.



Fig.11: Spiral inductor on pad-frame of 2µ process.

4. Conclusion

This project is a challenge problem in practical design. Because the higher inductor value L_s , the smaller Quality value Q that the chip can be. This design has met all desired parameters but the quality of Q due to the loss in substrate and materials. This design can be optimized by Adding more turns and using smaller outer dimensions. Since the number of turns increases, the self- inductance and mutual inductance also increase, but the series resistance decreases, the DC loss can be reduced. Otherwise, at the high frequency, the substrate loss limits the Q, and the substrate capacitance lowers the self-resonant frequency of the structure. Clearly, utilizing thicker oxide and lower permittivity dielectric helps to reduce the capacitance. The substrate loss can be reduced by eliminating the substrate resistance. This can be done by either shorting out the substrate resistance or by opening circuit. Anyway, the main drawback of spiral inductors is their low Q when compared to air-wound coils occupying comparable circuit board area. Their main advantage are near zero cost, low tolerance value, excellent repeatability, good temperature performance, and low susceptibility to mechanical vibration.

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