

Search-Based Design of Digital Non-Foster Antenna Match for High-Speed Low-Impedance Converters

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Abstract—Previous design procedures for low-frequency digital non-Foster circuits are most effective when high input impedance analog-to-digital converters are employed. However, these earlier design methods did not include the effects of potentially low impedances of high-frequency converters that may be required for antenna impedance matching. Therefore, we present a new search-based design procedure for digital non-Foster antenna-matching circuits using low-impedance converters. An example of the new design method is presented, with simulation results showing effective impedance matching of a 10 MHz electrically-small antenna using a digital non-Foster circuit and a low-impedance converter.

I. INTRODUCTION

The bandwidth of passively matched electrically-small antennas are constrained by the Wheeler-Chu limit [1]. A number of analog and digital non-Foster approaches have been proposed [2]–[4] to overcome the Wheeler-Chu limit. However, prior digital non-Foster design methods did not incorporate the effects of low impedances of high-frequency ADCs (analog-to-digital converter). Therefore, we propose a new search-based design procedure for digital non-Foster impedance matching of antennas, where low-impedance high-speed converters are employed.

II. DIGITAL NON-FOSTER APPROACH

A block diagram of a system for impedance matching of an antenna is shown in Fig. 1. The impedance of the digital non-Foster circuit in the large dashed box is in series with antenna impedance, $Z_A(s)$. A test source with impedance, $R_T = Re\{Z_A(s)\}$ is included for measuring s-parameters.

The voltage at the input of the non-Foster circuit, $V_{nf}(s)$, is digitized by the ADC with input resistance R_{adc} and sampling time, $T = 10$ ns to form $V_{nf}[n]$. The current of the digital non-Foster circuit is, $I_{nf}(s) = V_{nf}(s)/R_{adc} + [V_{nf}(s) - V_{dac}(s)]/[R_{io} + R_{dac}]$. The impedance of the digital non-Foster circuit, $Z_{nf}(s) = V_{nf}(s)/I_{nf}(s)$, is

$$Z_{nf}(s) \approx \frac{sTR_{adc}(R_{io} + R_{dac})}{sT(R_{adc} + R_{io} + R_{dac}) - R_{adc}H(z)(1 - z^{-1})} \Big|_{z=e^{sT}} \quad (1)$$

where $V_{nf}(t)$ is sampled without aliasing [4]. For the proposed search-based design procedure $H(z)$ is presumed to be:

$$H(z) = \frac{b_0z^2 + b_1z + b_2}{z^2 + a_1z + a_2} \quad (2)$$

where b_0, b_1, b_2, a_1, a_2 are real numbers.

III. SEARCH-BASED STABLE DESIGN APPROACH

As noted earlier, prior digital non-Foster design methods did not include effects of low-impedance (50Ω) converters. Therefore, we propose a search-based design method to find the parameters b_0, b_1, b_2, a_1, a_2 to match the antenna impedance. The search criteria is minimum error in the desired non-Foster impedance, $Z_{nf}(s)$, subject to the constraint of a stable system.

The flowchart in Fig. 2 describes the basic search procedure. The coefficients in (2) are searched over a range determined by the application, in the present case -25 to 25 , step size 0.25 . Then, each set of coefficients is checked for stability according to the characteristic equation described later. After checking for stability, coefficient sets with real part $Re\{Z_{nf}(s)\}$ outside the range of -3 to 3 are discarded, to preserve antenna efficiency. Next, a heuristic error measure $E = E^2(j\omega_1) + E^2(j\omega_2) + E^2(j\omega_3)$ for three frequencies is tested for each parameter set, where

$$E(s) = \frac{100|Im(Z_{nf}(s) - Z_d(s))|}{|Im(Z_d(s))|} + \frac{100|Re(Z_{nf}(s) - Z_d(s))|}{25|Re(Z_d(s))|} \quad (3)$$

$Im()$ and $Re()$ denote real and imaginary parts, and $Z_d(s)$ is the desired non-Foster matching impedance. Lastly, the minimum error solution is retained. A second pass is then done using a step size of 0.01 to refine the solution.

As noted above, the search-based method tests each set of coefficients for stability using poles of the characteristic equation of the system in Fig. 1, along the lines of [5]. The

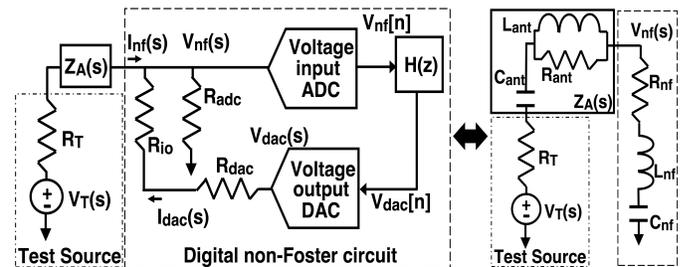


Fig. 1. Block diagram of digital non-Foster antenna matching circuit, with digital non-Foster approach of [4] modified to add low-impedance R_{adc} and R_{dac} , with antenna impedance $Z_A(s)$ and test source shown. Right: schematic illustrating desired digital non-Foster equivalent series-RLC R_{nf}, C_{nf} , and L_{nf} for antenna impedance match.

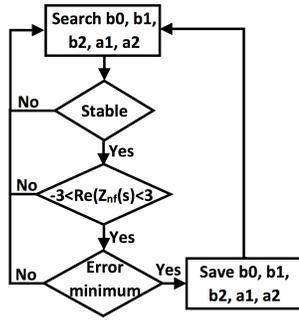


Fig. 2. Flowchart of proposed search-based design procedure for digital non-Foster circuits incorporating low-impedance converters.

system poles can be shown to be from the denominator of

$$\frac{C(z)}{R(z)} = \frac{H(z) \left(\frac{1}{R_{io} + R_{dac}} \right) Z_t(z)}{1 - H(z) \left(\frac{1}{R_{io} + R_{dac}} \right) Z_t(z)} \quad (4)$$

where $Z_t(z) = Z_A(s) || R_{dac} || (R_{io} + R_{dac})$, and $C(z)/R(z)$ is related to the closed loop response of the system of Fig. 1.

IV. SIMULATION RESULTS

This section presents simulation results for the wideband impedance matching of an electrically-small antenna with a digital non-Foster circuit including the effects of low-impedance converters. Below, we first describe how we obtain the desired impedance $Z_d(s)$ for (3). Then, we present simulation results showing that our search-based design of Fig. 3 provides a wideband non-Foster match to an electrically-small antenna.

First, the desired impedance $Z_d(s)$ of the series RLC circuit in Fig. 1 to provide a wideband non-Foster match to a 2 m long, 2 cm radius, electrically-small monopole at 10 MHz is obtained. At 10 MHz, the antenna impedance is $\approx 5 - j479 \Omega$ (≈ 33.2 pF). Based on the antenna impedance, the desired non-Foster matching impedance is determined using the procedure described in [4], for our example $C_{nf} = -37$ pF, $L_{nf} = 790$ nH and $R_{nf} = 2 \Omega$. **Antenna Cant=33.2 pF, Lant=480 nH, Rant=175 ohms.**

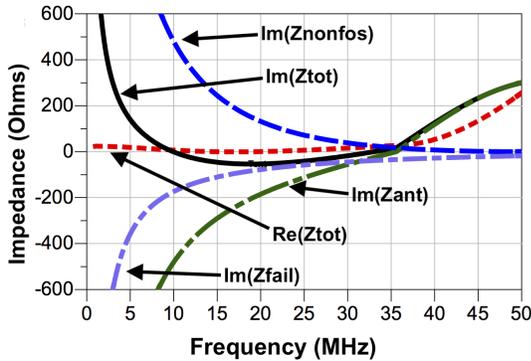


Fig. 3. Simulation results for impedance match of a 2.0 m long monopole antenna with proposed digital non-Foster design at operating frequency of 10 MHz, where $Re(Z_{tot})$ and $Im(Z_{tot})$ are resistance and reactance of the matched antenna impedance respectively. $Im(z_{ant})$ and $Im(Z_{nonfos})$ are the reactances of the antenna and digital non-Foster circuit, respectively.

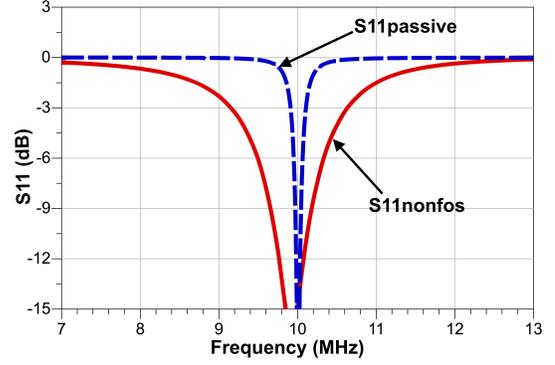


Fig. 4. Simulation results showing return loss of 2.0 m long monopole antenna with passive and proposed digital non-Foster impedance match. The 6 dB bandwidth for the passive match, $S_{11passive}$, is from 9.95 MHz to 10.06 MHz. The proposed digital non-Foster match, $S_{11nonfos}$, is from 9.49 MHz to 10.33 MHz.

Having determined the desired non-Foster impedance $Z_d(s)$, then $H(z)$ was designed using the search-based method of Fig. 2 with the three frequencies of error E being 9.5, 10, and 10.5 MHz in (3). The resulting $H(z)$ was

$$H(z) = \frac{12.11z^2 + 2.36z + 1.55}{z^2 + 1.77z + 0.79} \quad (5)$$

The impedance of the matched antenna is Z_{tot} shown in Fig. 3 with imaginary part $Im(Z_{tot})$ crossing zero near the desired 10 MHz operating frequency, indicating an effective impedance match of the monopole antenna. With $Z_{tot} = 6.6 - j1.4 \Omega$ at 10 MHz, the real part of Z_{tot} is 6.6Ω , and is denoted $Re(Z_{tot})$ in Fig. 3. Also shown is the imaginary part of the unmatched antenna $Im(Z_{ant})$ and the imaginary part of the digital non-Foster matching network $Im(Z_{nonfos})$, where $Im(Z_{nonfos}) \approx -Im(Z_{ant})$ at 10 MHz (The failed design using the earlier method in [4] is shown as $Im(Z_{fail})$).

The bandwidth improvement of the digital non-Foster antenna match using the new search-based design is shown in the S-parameters of Fig. 4, for the 5Ω test source shown in Fig. 1. Fig. 4 shows the digital non-Foster match with 6 dB bandwidth of 0.84 MHz, which is more than seven times the 0.11 MHz bandwidth of the passive match.

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