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# Exam1

ⓘ This is a preview of the draft version of the quiz

This exam is open book, open notes, you may use any online/hardback textbooks you like. You may use calculators and matlab, but may not collaborate with other people. All multiple choice answers should be within 5% of correct value.

**Unless stated otherwise in the question, use 3 decimal precision in fill-in-the blank questions, such as "132.312" or "58.023" for example. Do not give numerical fill-in-the-blank answers as fractions such as "4/5," give answer as decimal "0.800" form. Also, canvas might force you to enter a leading "0" for numbers less than one, such as "0.113" and entries such as ".113" might be disallowed.**

As always, make sure that you are in a location with good internet connectivity during the exam. It is not a bad idea to practice tethering through your cellphone as a backup to your regular internet access. Make sure your browser is compatible with canvas.

**Quiz Type** Graded Quiz

**Points** 150

**Assignment Group** Exams

**Shuffle Answers** Yes

**Time Limit** 75 Minutes

**Multiple Attempts** No

**View Responses** No

**One Question at a Time** No

**Require Respondus LockDown Browser** No

**Required to View Quiz Results** No

**Webcam Required** No

| Due              | For           | Available from | Until            |
|------------------|---------------|----------------|------------------|
| Apr 20 at 2:15pm | Everyone else | Apr 20 at 1pm  | Apr 20 at 2:15pm |
| Apr 20 at 3:30pm | 1 student     | Apr 20 at 1pm  | Apr 20 at 3:30pm |

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ⓘ Correct answers are hidden.

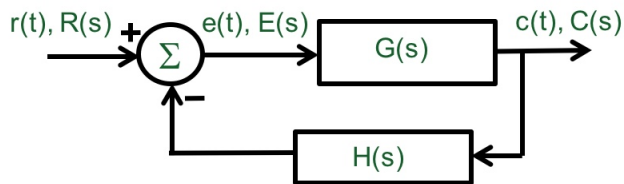
Score for this quiz: **150** out of 150

Submitted Apr 19 at 12:19pm

This attempt took 4 minutes.

**Question 1**

**5 / 5 pts**



For the continuous-time system above with  $H(s)=1/(s+2)$  and  $G(s)=5/(s+3)$ , the closed-loop transfer function is  $G_{CL}(s)=C(s)/R(s)=$

$\frac{5s+10}{s^2+5s+11}$

None above

$\frac{5(s+10)}{s^2+5s+12}$

$\frac{5s+2}{s^2+6s+11}$

$\frac{5(s+10)}{(s+5)(s+11)}$

$$= \frac{G(s)}{1+G(s)H(s)} = \frac{5/(s+3)}{1+5/((s+3)(s+2))}$$

$$= \frac{5(s+2)}{(s+3)(s+2)+5} = \frac{5s+10}{s^2+5s+11}$$

### Question 2

5 / 5 pts

If  $X(s) = \frac{3}{s(s+4)}$  then,  $x(t)=$

$3(1-e^{-4t})u(t)$

$(3/4)(1-e^{-4t})u(t)$

$(4/3)(1-e^{-4t})u(t)$

$4(1-e^{-3t})u(t)/3$

None above

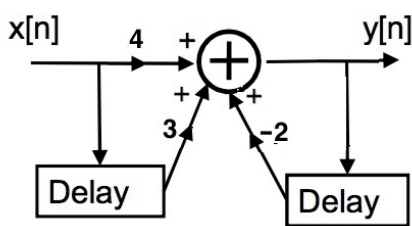
Laplace table

$$\frac{a}{s(s+a)} \Rightarrow (1-e^{-at})u(t)$$

$$\frac{3}{4} \frac{4}{s(s+4)} \Rightarrow \frac{3}{4}(1-e^{-4t})u(t)$$

### Question 3

5 / 5 pts



$$y[n] = -2y[n-1] + 4x[n] + 3x[n-1]$$

$$Y(z)(1 + 2z^{-1}) = X(z)(4 + 3z^{-1})$$

For the LTI system above with impulse response  $h[n]$ , the z-transform of  $h[n]$  is  $H(z)=Y(z)/X(z)=$

- $(3z+4)/(z-2)$
- $(4z+3)/(z+2)$
- $(2z+1)/(3z+4)$
- None above
- $(2z+1)/(4z-3)$

**Question 4**

5 / 5 pts

The z-transform of  $x[n]=(3/4)^{n-1} u[n-1]$  is

- $4z/(3z-9/4); |z|>3/4$
- None above
- $1/(z-3/4); |z|>3/4$
- $0.75z/(z-3/4); |z|>3/4$
- $0.75/(z-4/3); |z|>4/3$

$$\left(\frac{3}{4}\right)^n u[n] \Rightarrow \frac{z}{z-3/4}$$

$$\text{delay prop} \Rightarrow \frac{z^{-1}z}{z-3/4}$$

**Question 5**

5 / 5 pts

In a 10 sample/s system with  $X^*(s) = 1/(5 + e^{s/10})$  the z-transform (ignoring ROC) is  $X(z) =$

- $\frac{1}{z^2+5}$
- none above

$$e^{s/10} = z$$

$$\frac{1}{5 + (e^{s/10})^2} \Rightarrow \frac{1}{5 + z^2}$$

$\frac{z^2}{z^2+0.5}$

$\frac{5z}{z^2+5}$

$\frac{1}{z^{-2}+5}$

## Question 6

5 / 5 pts

In a 5 sample/s system with  $X(s)=4/s^2$ , the starred transform is  $X^*(s) =$

$\frac{0.2 e^{s/5}}{(e^{s/5}-4)^2}$

 none above

$\frac{e^{s/5}}{e^{s/5}-1}$

$\frac{0.8e^{s/5}}{(e^{s/5}-1)^2}$

$\frac{0.2 e^{-4/5}}{(e^{-s/5}-1)^2}$

$$x(t) = 4t u(t)$$

$$\Rightarrow x[n] = 4nT u[n]$$

$$X(z) = 4T \frac{z}{(z-1)^2}$$

$$X^*(s) = 4T \frac{e^{sT}}{(e^{sT}-1)^2} = \frac{4}{5} \frac{e^{s/5}}{(e^{s/5}-1)^2}$$

## Question 7

5 / 5 pts

A continuous-time signal  $x(t)$  is sampled with period  $T_0=0.1$  s to create discrete-time signal  $x[n]$ , and the z-transform of  $x[n]$  is  $X(z) = \frac{2}{3z-1}$ ;  $|z| > \frac{1}{3}$ . Then, the starred transform of  $x(t)$  is  $X^*(s) =$

$\frac{2}{3e^{s/10}-1}$

$\frac{2e^{s/10}}{3-e^{s/10}}$

$\frac{2e^{-s/10}}{3e^{-s/10}-e^{-1/10}}$

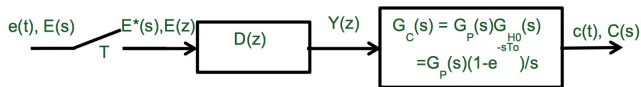
 None above

$\frac{2}{3e^{-s/10}-1}$

$$\frac{2}{3z-1} \Big|_{z=e^{sT}} = \frac{2}{3e^{s/10}-1}$$

**Question 8**

5 / 5 pts



In the system above, let  $T=0.1$  s,  $D(z)=1-1/z$ ,  $G_p(s)=4/(s+4)$ ,  $G_{H0}(s)=(1-e^{-sT})/s$ .

For the system above, the pulse transfer function is  $G(z)=C(z)/E(z)=$

$(1+1/z)(1+e^{-4/5})/(z-e^{-4/5})$

$(1-1/z)(1-e^{-2/5})/(z-e^{-2/5})$

None above

$(4/10)(1+e^{-2/5})/(z+e^{-2/5})$

$(2/5)(1-e^{-5/2})/(z-e^{-5/2})$

Handwritten work for Question 8:

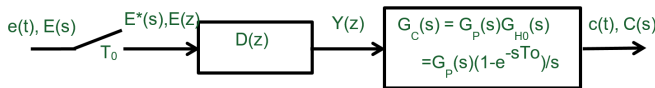
$$G'(s) = \frac{4}{s+4} \frac{1-e^{-sT}}{s} = \left(1-\frac{1}{z}\right) \frac{4}{s(s+4)} \cdot 1-e^{-sT}$$

$$\Rightarrow \left(1-\frac{1}{z}\right) \frac{z(1-e^{-4T})}{(z-1)(z-e^{-4T})} \frac{z-1}{z}$$

$$G'(z) = \left(1-\frac{1}{z}\right) \frac{1-e^{-4/10}}{z-e^{-4/10}}$$

**Question 9**

5 / 5 pts



For the system above,  $D(z) = 1-0.5z^{-1}$ ,  $G_p(s)=3/s$ ,  $G_{H0}(s)=(1+e^{-sT0})/s$ ,  $T_0=1/10$

In the open-loop system above, the starred transform of the output is  $C^*(s)=$

none of the answers

$\left(\frac{4}{5}\right) \frac{2e^{s/10}+1}{e^{s/10}(e^{s/10}-1)} E^*(s)$

$\left(\frac{3}{20}\right) \frac{2e^{s/10}-1}{e^{s/10}(e^{s/10}-1)} E^*(s)$

$\left(\frac{4}{5}\right) \frac{e^{s/10}-2}{e^{s/10}(e^{s/5}-1)} E^*(s)$

Handwritten work for Question 9:

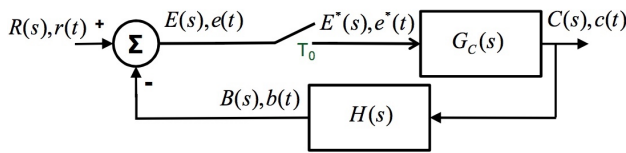
$$G'(s) = \frac{3}{s} \frac{1+e^{-sT_0}}{s} = \frac{z-1/2}{z} \frac{3}{s^2} (1+e^{-sT_0})$$

$$\frac{z-1/2}{z} \frac{3}{s^2} \frac{zT}{z-1} \frac{z-1}{z} = \frac{2z-1}{2z} \frac{3/10}{z-1}$$

$$G'(z) = \frac{3}{20} \frac{2z-1}{z(z-1)} \Big|_{z=e^{sT_0}=e^{s/10}}$$

**Question 10**

5 / 5 pts



$$G_c(s) = 15 \frac{1 - e^{-sT}}{s} = \frac{15}{s} (1 - e^{-sT})$$

$$G_c(z) = 15 \frac{z - z^{-1}}{z - 1} = 15$$

In the system above, let:

$H(s) = 1/10$ ,  $G_C(s) = G_P(s)G_{H0}(s)$ ,  $G_P(s) = 15$ ,  $G_{H0}(s) = (1 - e^{-sT})/s$ .

$$\frac{C(z)}{R(z)} = \frac{G_c(z)}{1 + G_c H(z)} = \frac{15}{1 + 15/10} = \frac{150}{25} = 6$$

The closed-loop continuous-time step response is

- 1.6 u(t)
- 3 u(t)
- 6 u(t)
- None above

$$C(s) = E^*(s) G_c(s)$$

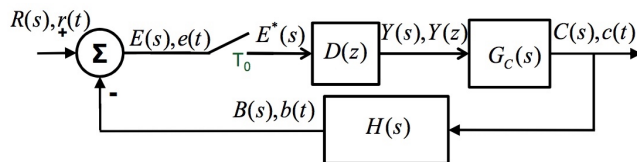
$$E^*(s) = R^*(s) - E^* G^* H^* \Rightarrow E^* = \frac{R^*}{1 + G^* H^*}$$

$$C(s) = \frac{R^* G_c(s)}{1 + G_c H^*} = \frac{z \cdot 15 \cdot \frac{z-1}{z}}{1 + 15/10}$$

$$= \frac{15}{2.5} \cdot \frac{1}{z} = 6 \cdot \frac{1}{z}$$

Question 11

5 / 5 pts



If the characteristic equation for the system above is

$$z^2 + z - 5/16 = 0,$$

then the closed-loop pulse transfer function  $G_{CL}(z) = C(z)/R(z)$  is stable.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

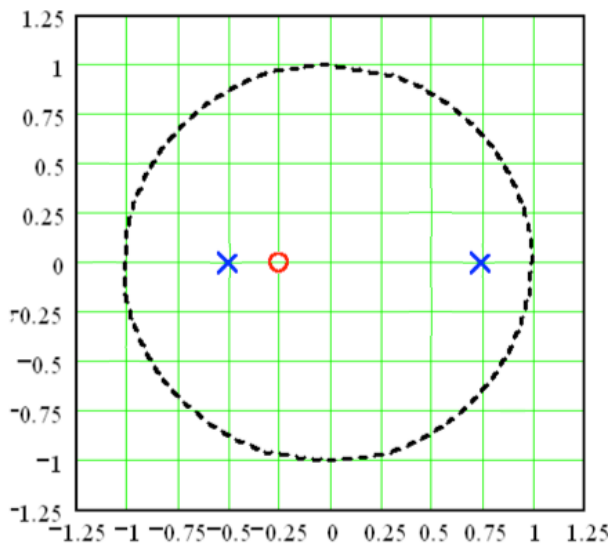
$$= \frac{-1 \pm \sqrt{1 + 20/16}}{2}$$

$$= \frac{-1}{2} \pm \frac{\sqrt{36/16}}{2} = \frac{-1}{2} \pm \frac{3}{4}$$

- True
- False

Question 12

5 / 5 pts



The causal LTI system with closed-loop pulse transfer function  $G_{CL}(z)$  having the pole/zero plot above is BIBO stable.

- True
- False

**Question 13**

5 / 5 pts

For a system with variable gain  $K > 0$ , the closed-loop response  $G_{CL}(z) = \frac{C(z)}{R(z)} = \frac{\frac{K}{2z+4}}{1 - \frac{K}{2z+4}}$  is stable for

- $2 < K < 4$
- $2 < K < 6$
- $0 < K < 2$
- none of the answers

$$= \frac{K}{2z+4-K}$$

$$= \frac{K/2}{z+2-K/2}$$

Real Pole @  $z = \frac{K}{2} - 2$

Pole @ 1 for  $z=6$ , @ -1 for  $z=2$

**Question 14**

5 / 5 pts

The w-transform of  $1/(3z-4)$  in a 5 sample/s system is

- none of the answers

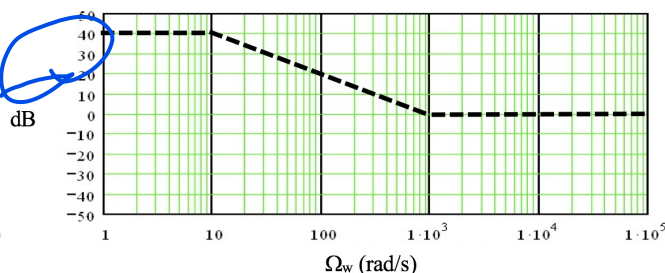
$$\frac{1}{3\left(\frac{1+W T/2}{1-W T/2}\right) - 4} = \frac{1-W/10}{3 + \frac{3W}{10} - 4 + \frac{4W}{10}}$$

$$= \frac{10-W}{30+3W-40+4W}$$

- $\frac{4-3w}{21w-4}$
- $\frac{5-2w}{14w-5}$
- $\frac{10-w}{7w-10}$

**Question 15**

5 / 5 pts



For the  $w$ -transform of the digital lag filter with  $|D(w)|$  shown above,  $D(w) =$

$$100 \frac{1 + w/1000}{1 + w/10}$$

$$= 100 \frac{1000(w+1000)}{10(10+w)}$$

- None above
- $0.1(w+10)/(w+1000)$
- $0.3(w+1000)/(w+10)$
- $100(w+1000)/(w+10)$
- $(w+1000)/(w+10)$

**Question 16**

5 / 5 pts

For a lag compensator with  $D(w) = 4 \frac{1 + \frac{w}{16}}{1 + \frac{w}{2}}$  in a system with sample period  $T_s = 1/4$  s, the corresponding discrete-time compensator is  $D(z) =$

$$D(z) = \left( a_0 \frac{w_p}{w_0} \left( \frac{1 + w_0 T / z}{1 - w_p T / z} \right) \frac{z - (1 - w_0 T / z)}{z - (1 - w_p T / z)} \right)$$

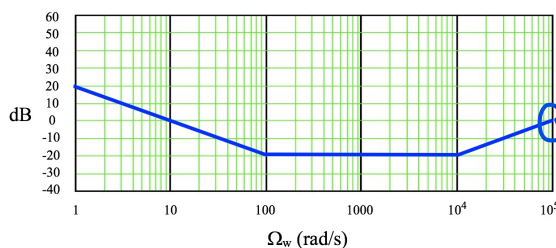
Handwritten annotations:  $a_0 = 4$ ,  $w_0 = 16$ ,  $w_p = 2$ ,  $T = 1/4$

- $(10z - 2)/(z + 3)$
- none of the answers
- $(8z + 4)/(6z - 3)$
- $(6z + 2)/(5z - 3)$



Question 17

5 / 5 pts



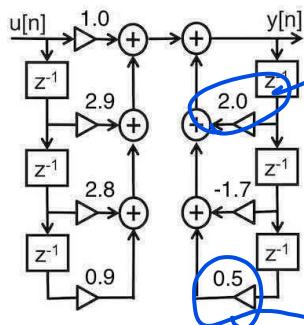
For the w-transform of the PID controller with  $|D(w)|$  shown above, to within +/- 20% the differentiator coefficient is  $K_D =$

$$|K_D \omega| = |K_D \cdot 10^5| = 1$$

- None above
- 0.1
- 10
- $10^{-5}$
- 1,000

Question 18

5 / 5 pts



$$\begin{bmatrix}
 0 & 1 & 0 \\
 0 & 0 & 1 \\
 -a_3 & -a_2 & -a_1
 \end{bmatrix}$$

Handwritten annotations:  $-a_1$  points to the top-right element (0),  $-a_2$  points to the middle-right element (0),  $-a_3$  points to the bottom-left element (-1.7), and  $0.5$  points to the gain of the feedback path.

For the digital system above with sample period  $T_s = 0.001$  s, controllable form state-variable matrix  $A =$

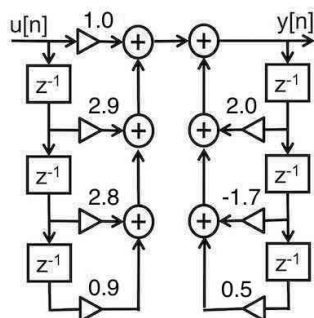
- $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 2 & -1.7 & 0.5 \end{bmatrix}$
- none of the answers
- $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0.9 & 2.8 & 2.8 \end{bmatrix}$

$\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -0.5 & 1.7 & -2 \end{bmatrix}$

$\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0.5 & -1.7 & 2 \end{bmatrix}$

## Question 19

5 / 5 pts



$$\begin{bmatrix} B & AB & A^2B \end{bmatrix}$$

For the digital system above with sample period  $T_0=0.001$  s, the controllability matrix is

$\begin{bmatrix} 0 & 0 & 0.5 \\ 0 & 1 & 1 \\ 1 & 0.9 & 1.9 \end{bmatrix}$

$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 2 & 2.3 \end{bmatrix}$

$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 1.7 & -1.1 \end{bmatrix}$

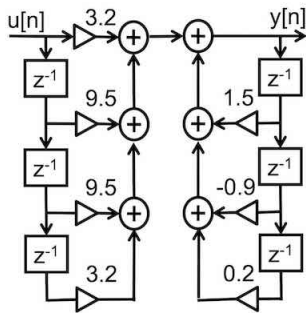
$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ -2.9 & -2.8 & -0.9 \end{bmatrix}$

none of the answers

$$= \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 2 & 2.3 \end{bmatrix}$$

## Question 20

5 / 5 pts



Control Matrix HAS INVERSE

For the digital system above with sample period  $T_0=0.001$  s, the system is controllable.

- True
- False

**Question 21**

5 / 5 pts

A state-variable system with observability matrix  $\begin{bmatrix} -1 & 1 \\ 2 & -2 \end{bmatrix}$  is observable.

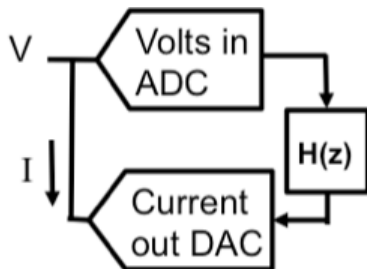
- True

Rank = 1

- False

**Question 22**

5 / 5 pts



$\frac{C}{T} = -20$   
 $C = \frac{-20}{1000}$

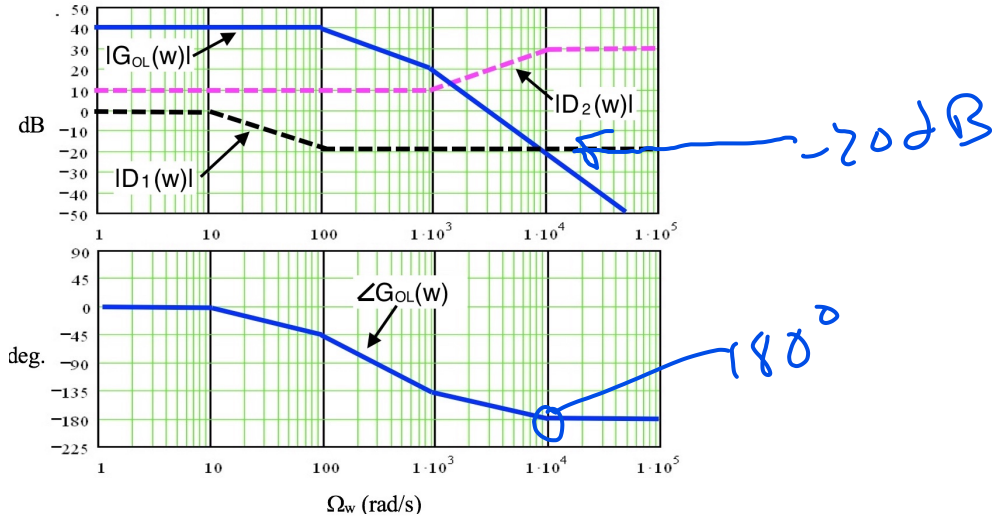
If  $H(z) = -20(1 - z^{-1})$  and  $T_0 = 10^{-3}$  s for the system above, and for the direction of DAC current as shown, the input capacitance in seen at the point V is

- none of the answers
- 0.02 F

- 0.005
- 0.02 F
- 0.005 F

**Question 23**

5 / 5 pts

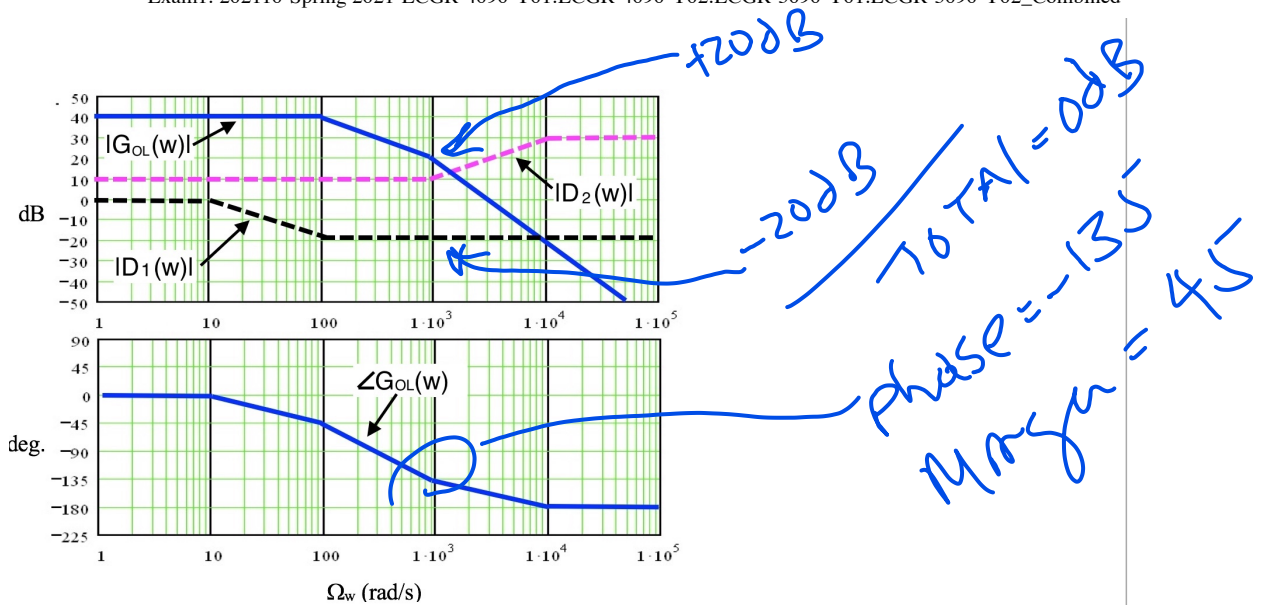


For the w-transforms shown above, the Bode plots for phase of the two compensators are not shown (you may assume the phases are the correct Bode plot phases for lag, lag-lead, PID, or lag compensators). For **uncompensated** open-loop gain G<sub>OL</sub>(w) shown above, using Bode plot analysis the gain margin to within +/-3 dB is

- 0 dB
- 10 dB
- none of the answers
- 20 dB

**Question 24**

5 / 5 pts

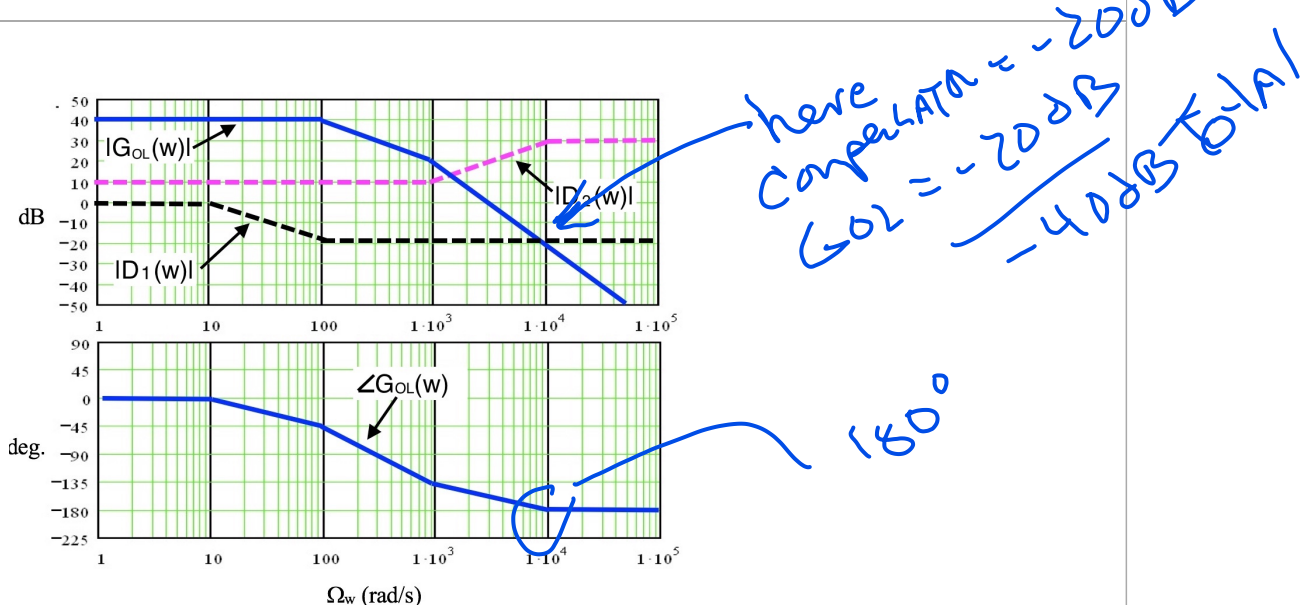


For the  $w$ -transforms shown above, the Bode plots for phase of the two compensators are not shown (you may assume the phases are the correct Bode plot phases for lag, lag-lead, PID, or lag compensators). For open-loop gain  $G_{OL}(w)$  combined with compensator  $D_1(w)$  shown above, the phase margin of  $G_{OL}(w)D_1(w)$  to within  $\pm 10$  degrees is

- 135 degrees
- 45 degrees
- none above
- 90 degrees

Question 25

5 / 5 pts



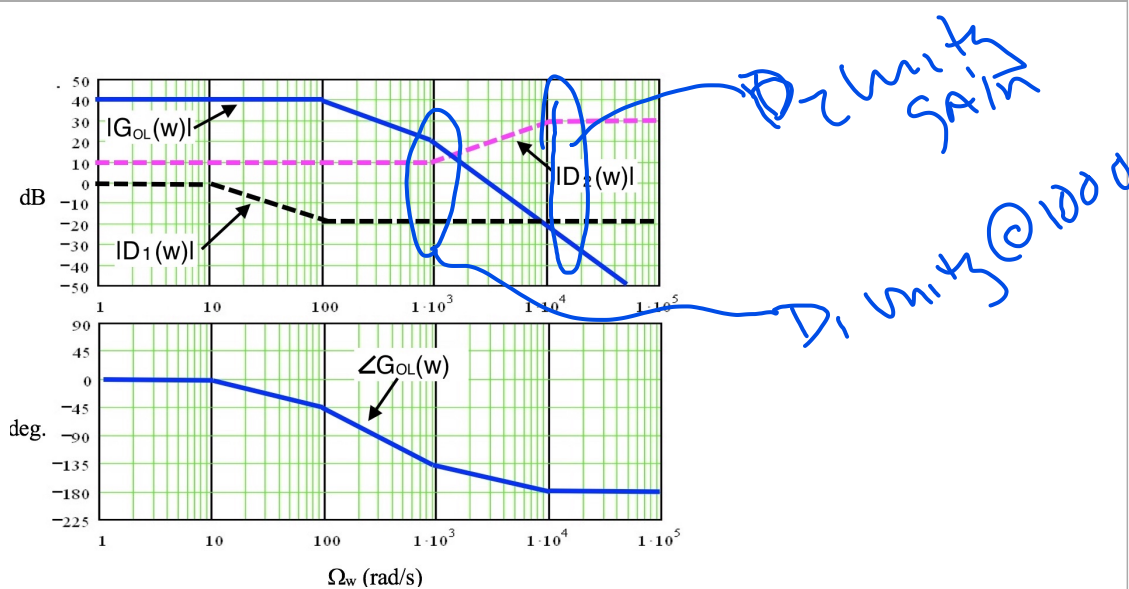
For the  $w$ -transforms shown above, the Bode plots for phase of the two compensators are not shown (you may assume the phases are the correct Bode plot phases for lag, lag-lead, PID, or lag

compensators). For open-loop gain  $G_{OL}(w)$  combined with compensator  $D_1(w)$  shown above, the gain margin of  $G_{OL}(w)D_1(w)$  to within  $\pm 4$  dB is

- 20 dB
- 60 dB
- 40 dB
- None above

**Question 26**

5 / 5 pts

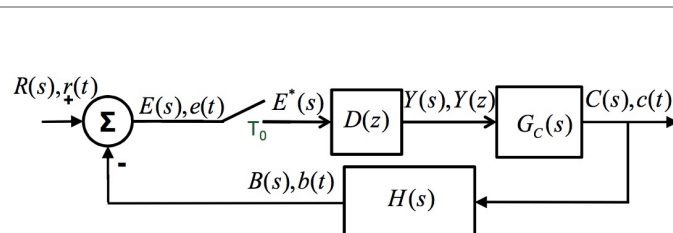


For the  $w$ -transforms shown above, the Bode plots for phase of the two compensators are not shown (you may assume the phases are the correct Bode plot phases for lag, lag-lead, PID, or lag compensators). For open-loop gain  $G_{OL}(w)$ , comparing the bandwidth using the two compensators, the unity-gain bandwidth of  $G_{OL}(w)D_1(w)$  is larger than  $G_{OL}(w)D_2(w)$ .

- True
- False

**Question 27**

5 / 5 pts



In the system above, let

$D(z)=2-1/z, H(s)=1/5, G_C(s)=G_P(s)G_{H0}(s), G_P(s)=20, G_{H0}(s)=(1-e^{-sT})/s.$

For the system above, the closed-loop pulse transfer function is  $G_{CL}(z)=C(z)/R(z)=$

$= \frac{2z-1}{z}$

$10(2+1/z)(1+e^{-T_0})/(4z-9)$

$20(2-e^{-5T_0})/(z-e^{-5T_0})$

None above

$2(z+20)/(z+8/9)$

$20(2z-1)/(9z-4)$

$(20z+1)/(z^2+z+1/4)$

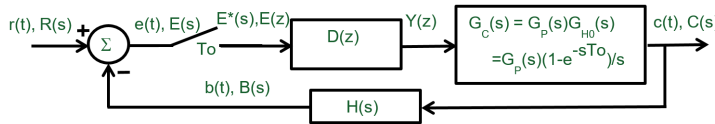
$G_c(s) = 20 \frac{(1-e^{-sT})}{s} = \frac{20}{s} (1-e^{-sT})$

$G_c(z) = \frac{20z}{z-1} \frac{z-1}{z} = 20$

$G_{CL}(z) = \frac{D(z)G_c(z)}{1+D(z)G_c(z)} = \frac{\frac{2z-1}{z} \cdot 20}{1 + \frac{2z-1}{z} \cdot 20} = \frac{20(2z-1)}{z+20(2z-1)} = \frac{20(2z-1)}{9z-4}$

**Question 28**

5 / 5 pts



For the system above:

In the system above, let

$D(z)=2-1/z, H(s)=1/5, G_C(s)=G_P(s)G_{H0}(s), G_P(s)=20, G_{H0}(s)=(1-e^{-sT})/s.$

For the system above, the pole of the closed-loop pulse transfer function  $G_{CL}(z)$  is at

-0.25

0.63

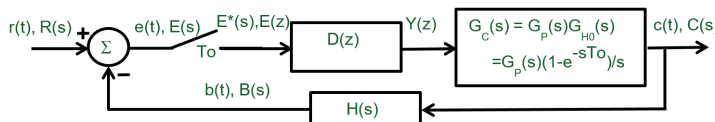
none of the answers

0.44

$z = \frac{4}{9} \approx .44$

**Question 29**

5 / 5 pts



For the system above:  $D(z) = 1 - 0.5z^{-1}$ ,  $G_P(s) = 8/s$ ,  $G_{H0}(s) = (1 + e^{-sT_0})/s$ ,  $H(s) = 1/2$ ,  $T_0 = 1/5$

For the system above, the closed loop pulse transfer function is  $G_{CL}(z) = C(z)/R(z) =$

$= \frac{z - 1/2}{z}$

- $\frac{8z-4}{5z^2 - z - 2}$
- $\frac{8z-2}{7z^2 + 2z - 6}$
- none of the answers
- $\frac{z-4}{8z^2 - 4z - 2}$

$G_C(s) = \frac{8}{s} \frac{1 - e^{-5T}}{s} \Rightarrow \frac{8}{s^2} (1 - e^{-5T})$

$G(z) = \frac{8Tz}{(z-1)^2} \frac{z-1}{z} = \frac{8/5}{z-1}$

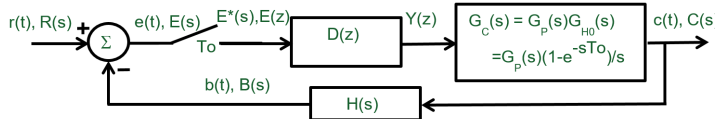
$G_{CL}(z) = \frac{D(z)G_C(z)}{1 + D(z)G_C(z)H(z)} = \frac{z-1/2 \cdot 8/5}{1 + \frac{z-1/2 \cdot 8/5}{z} \cdot \frac{1}{2}}$

$= \frac{8z-4}{5z^2 - 5z + 4z - 2} = \frac{8z-4}{5z^2 - z - 2}$

$G'(s)$

Question 30

5 / 5 pts



$\frac{+1 \pm \sqrt{1^2 + 40}}{10}$

For the system above:  $D(z) = 1 - 0.5z^{-1}$ ,  $G_P(s) = 8/s$ ,  $G_{H0}(s) = (1 + e^{-sT_0})/s$ ,  $H(s) = 1/2$ ,  $T_0 = 1/5$

For the system above, the poles of the closed-loop pulse transfer function  $G_{CL}(z)$  are at

- 0.32 and 0.65
- 0.53 and 0.21
- none of the answers
- 0.74 and -0.54

Quiz Score: 150 out of 150